

A NEW APPROACH TO THE ESTIMATION OF PARAMETERS IN LINEAR MODELS

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ABSTRACT

In this paper we attempt to forward a new approach for the estimation of parameters in linear models. This approach leads to identifiable parameters which is a problem in some models. Some examples are also provided.

INTRODUCTION

Suppose that two non-stochastic variables X and Y obey the linear relation

$$Y = \alpha + \beta X \quad (1)$$

and we wish to obtain values for the parameters α and β . If we observe only the stochastic variables, A and B where

$$A = X + C, \text{ and } B = Y + D \quad (2)$$

where C and D are random disturbances then the least squares model is no longer valid, while if A and B are treated as normal variates, there is a lack of identifiability among the parameters. Various methods have been proposed to deal with this situation. These are reviewed in [1,2].

To make all the parameters in this model identifiable, we may either restrict the parameter values in some way or else increase the amount of available information. In particular, this situation may arise where two readings A_1 and A_2 are available.

SPECIFICATION OF THE MODEL

We have n triads of observations (A_{1i}, A_{2i}, B_i) , $i = 1, 2, \dots, n$ where